

Search

Agents

Agents interest of
complete process
(simple system)

Agents interest of what
will happen after ending
the process of find
best solution.
(complex system)

1) Reflex agent (simple system)

- a) choose action based on current percept.
- b) may have memory or model of world's current state.
- c) Do not consider future consequence of their actions.
"Do not ask ~~if~~ what if"
- d) Consider how the world is (cannot care
about future actions)
- e) Can it be rational (yes)?
↳ yes, if it is provided by if conditions.

2] Planning Agents (complex system)

- a) Ask "what-if"
- b) Decisions based on (hypothesized) consequences of actions.
- c) must have model of how world evolves in response to actions.
- d) must formulate a goal (test) \Rightarrow must reach the goal.
- e) consider how the world would be.

Planning	Replanning
→ Agent make Plan according to search.	→ Agents make Plan for the first step according to search then take decision to complete first step. <u>then</u>
→ It take period of time to plan then take decision according to plan.	→ It replan for next step according to new search and take new best decision to start work for next step.
→ Plan only one time	→ Plan for each step ↳ no. of plans = no. of steps.

*optimal vs complete Planning

↳ Agent, not only reach goal or take action but also it want to get optimal solution of problem. (Search for best way to goal or minimum time to reach goal)

*Search Problems:

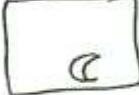
↳ process to take right decision.

It consists of

1) state space (world): All possible cases of the model.

ex mouse want to eat 9 piece of cheese.

 → mouse eat piece on center

 → eat the last piece.

2) A Successor Function (actions, costs)

↳ For any state what action can I take and what cost of taking it.

3) A start state an goal test

start state: state from which i can start working.

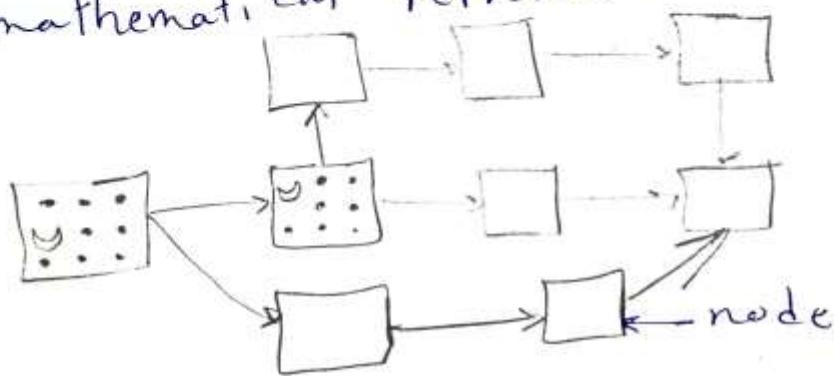
goal test: the final state.

→ solution of search problem is sequence of action which transforms start state to goal state.

*Uniformed search methods

① state space representation

→ mathematical representation of search problem.



• nodes → world configurations.

• Arc → successors (action results)

• goal test is set of goal nodes.

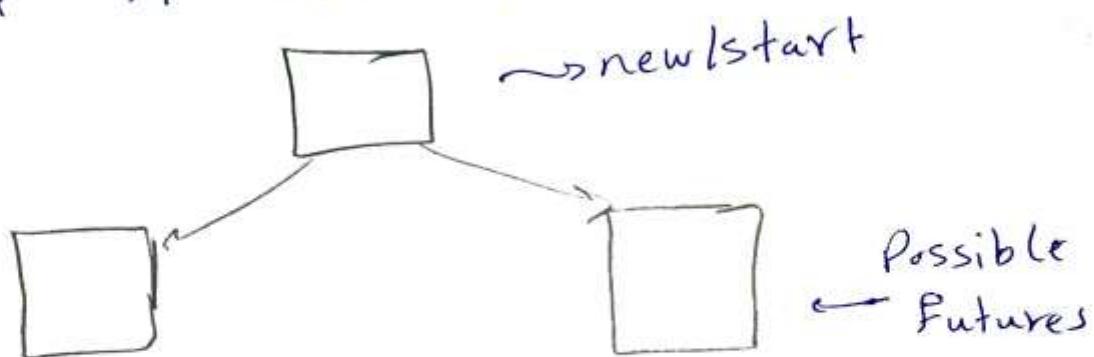
→ here we represent needed states only.

→ we can rarely build this full graph.

→ there is no start state. but goal test.

② Search trees

↳ part of search graph.



Search tree

- start state is the root node.
- children correspond to successors.
- we can never actually build whole tree.

* searching with search tree

- a) try to expand as few tree nodes as possible
- b) maintain a fringe of partial plans under consideration.
- c) try to expand as few tree nodes as possible

(General Tree Search)

Frings : all of plans that may yet work.

- all ways that can reach me from start to goal during world state search tree.

→ one of this frings is my solution (^{optimal} solution)

Expansion

↳ picking some thing out of the fringe and if it is not a goal already.

→ process of expanding new state from current state on one of frings. we can't do this process if we reach goal.

* Exploration strategy

↳ what fringe nodes do you explore next?
↳ what will happen next?

* Main Question:-

↳ which fringe nodes to explore to reach goal?

Depth-First Search

strategy: expand deepest node first

Implementation: fringe is LIFO stack.

Solution: left most solution.

Search Algorithm Properties

→ For any Algorithm we check For 4 Properties:-

1] Complete:

↳ Ability to reach goal if it is exist.

2] Optimal:

↳ Ability to reach to best solution.

3] Time Complexity

↳ time to reach to solution

↳ time to expand all nodes of one fringe equal to time to expand one node of fringe * no. of fringe nodes.

4] Space Complexity

↳ size of fringe in memory. size of nodes of fringe in stack.

* no. of nodes in entire tree.

$$1 + b + b^2 + \dots + b^m = O(b^m)$$

→ branching factor: start node can make a branch for b number of children.

Depth First Properties

1] Time complexity

- what nodes DFS expand?
 - ↳ some left prefix of tree.
 - ↳ could process the whole tree!
- ↳ worst case expand all nodes (right most)
 - ↳ best case expand no nodes (start \equiv goal)

worst case: $O(b^m)$, best case = $O(1)$

2] Space complexity

- ↳ only has siblings on path to root, so $O(b^m)$
- ↳ worst case we get solution on last tier.

3] Complete

- ↳ m could be finite, if we prevent cycles.
- solution can only be found if
 - 1. it is exist
 - 2. finite Algorithm.

4] optimal

- no, ~~it~~ it finds left most solution regardless of depth or cost.

2] Breadth -First (BFS)

strategy: expand a shallowest node first.

Implementation: fringe is FIFO queue.

solution: shallowest solution (shortest fringe)

*

*DFS & BFS

→ BFS will outperform DFS when:

- 1) need less time complexity.
- 2) need shallowest solution.
- 3) need optimal solutions for costs equal to 1.
- 4) need complete solutions.

→ DFS will outperform BFS when:

- 1) most solutions at left side of tree.
- 2) all ~~solutions~~ at the last level.
- 3) need less space complexity.



3) uniform cost

strategy: expand a cheapest node first.

Implementation: fringe is priority queue

solution: cheapest solution.

→ expand node of cheapest cost.

*Advantages

→ complete and optimal.

*Disadvantages

1. no information about goal location.

(expand) after knowing (goal) ~~Nodes, no need to visit with nodes in~~

2. explores options in every direction.

↳ no determined direction on our work.

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* The one queue: Priority queues

- conceptually, all frings are priority queues.
- For DFS and BFS you can avoid the $\log(n)$ overhead from actual priority queue with stacks and queues.
- Can even code one implementation that takes variable queuing object.

Informed search

↳ we need to know information about goal location to know if I work on correct way or not.

→ we have one function, 2 search Algorithms.

1) Heuristics

↳ function takes state of state space, and give number which represent how far the goal location from my location to doing process.

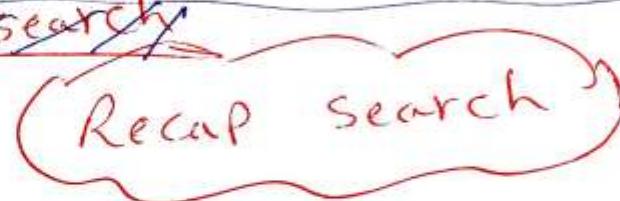
* Greedy search

- ↳ Search Algorithm use idea of Heuristic.
- ↳ It is not an optimal search Algorithm

* A* search

- ↳ It collects all last search Algorithms ideas to get very good search Algorithm.

* Graph search



1) Search Problem

- a) states (configuration of world)
- b) actions & costs.
- c) successor function (say how states respond to actions)
- d) start state & goal state.

2) Search tree

↳ nodes: Plans for reaching states.

↳ plans have costs (sum of action costs)

3) Search Algorithm

↳ systematically builds search tree.

↳ chooses an ordering of the fringe.

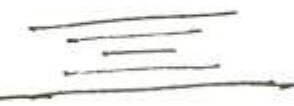
↳ optimal: find the least-cost plans.

Ex: Pancake Problem

problem: need to arrange pancake from big to small.

states: shape of pancakes during flipping to reach goal.

costs: no. of pancakes flipped.

start state: 

goal state: 

Algorithm: we can use UCS algorithm according to cost also we can use DFS or BFs.

Search Heuristics

heuristic is

- a) Function that estimates how close a state to goal.
- b) Designed for particular search problem.
- c) we make it every step to see if it is close to goal or not.
- d) every search problem need different heuristic according to nature of problem.

Heuristics

Heuristic: no. of largest pancake that is still out of place.

Greedy search

strategy: expand the nodes that seems closest to goal according to heuristic.

Heuristic: estimate the distance to nearest goal for each state.

Implementation: Priority queue ℓ :

solution: best heuristic solution.

→ It doesn't care about cost.
→ cares only about heuristic

~~common case~~: best-first takes you to wrong goal.

worst case: like badly-guided DFS.

solution → combine UCS and Greedy search.

A* search

→ combining UCS and Greedy Search.

uniform cost orders by path cost or backward cost $g(n)$.

Greedy search is by goal proximity or forward cost $h(n)$.

↳ should we stop when we enqueue goal?

↳ No only stop when we dequeue goal.

Admissibility

- * Inadmissible (Pessimistic) heuristics break optimality by trapping good plans on fringe.
- * Admissible (optimistic) heuristics slow down bad plans but plans never outweigh true costs.

(Admissible heuristic)

~ A heuristic h is admissible if:

$$0 \leq h(n) \leq h^*(n) \rightarrow h^*(n) = g(n)$$

~ $h^*(n)$ is true cost to nearest goal

$h(n) > h^*(n) \rightarrow$ (optimal) n is not a solution

* A* applications

* Video games. * language analysis.

* Machine translation * speech recognition.

* Robot motion Planning.

* Resource Planning Problems.

* Creating Admissible heuristics

- most of work in solving hard search problems optimally is in coming up with admissible heuristics.
- often, admissible heuristics are solutions to relaxed problems where new actions are available.
- inadmissible heuristics are often useful too.

Ex 8 Puzzle

7	2	4
5	6	
8	3	1

start state

3	7	1
2	4	5
	6	

Action

	1	2
3	4	5
6	7	8

Goal state

states? all cases that i can move any number from its location to another one if it is next to free space

How many states $\rightarrow 8! =$

actions? moving number to free space next to it.

- * no. of successors from start state?
- maximum 4 moves (minimum 2 moves)
- * cost should be? 1 every time
- * heuristic: no. of tiles misplaced.

$$h(\text{start}) = 8$$

- * why it is admissible?

1) There is relaxed-problem heuristic
(easiest solution but need more work)

2) Direct move
↳ move every number from start state to final state.

$h = \text{no. of moves}$
 $h(1) = 3$ (moves to reach to its correct state at goal state)

$$h(2) = 1, h(3) = 2 \text{ and so on.}$$

↳ Total $h = 18$ from start to goal.

Admissible if $0 \leq h(n) \leq 2(n)$

~ How about using actual cost as heuristic?

$$f(n) = h(n) + g(n) = 2g(n) = 2h(n)$$

$$\text{if } g(n) = h(n)$$

↳ we go back to UCS by double cost
value trade off: complex work, neglect heuristic

with A* → trade off - between quality of
estimate and work per-node

* Trivial heuristic

• bottom of lattice is zero heuristic

• top " " is the exact " if $h=0$ no heuristic \Rightarrow go back to $\begin{cases} \text{uniform} \\ \text{cost} \\ \text{search} \end{cases}$

Dominance: $h_a \leq h_c$

$\forall n: h_a(n) \geq h_c(n)$ for all nodes

we choose $h_a(n)$ (best one)

→ Heuristics from a semi-lattice

↳ max of admissible heuristics is admissible

$$h(n) = \max(h_a(n), h_b(n))$$

we choose

Graph search

↳ Failure to detect repeated states can cause exponential more work.
Idea: never expand state twice.

Implementation:

- * tree search + set of expanded states (^{closest} set)
- * expand search tree node by node, but never expand node twice.
- * Before expanding a node, check if it is expanded before or not.
- * if not now, skip it, if new add to closest set.

Important

- * store closest set as a set, not a list.
- * complete ~ if goal exists, we will find it.
- * optimal ~ no.

(19)

	Depth First Search	Breadth First search	Uniform Cost search
nodes expanded	<ul style="list-style-type: none"> → Some left prefix of the tree. → Could process the whole tree. → if m is infinite, takes time $O(b^m)$ 	<ul style="list-style-type: none"> → Processes all nodes above shallowst solution. → Let depth of shallowst solution be s. → Search takes time $O(b^s)$ 	<ul style="list-style-type: none"> → Process all nodes with cost less than cheapest solution. → Takes time $O(C^*/\epsilon)$ C^* → sol. costs ϵ.
space that strings take	$O(b^m)$	$O(b^s)$	$O(b^{C^*/\epsilon})$
complete	only if we prevent cycles	$s \rightarrow$ finite Yes	Assume best sol. has finite cost and min. ϵ → Yes
optimal	No	only if costs are all 1	Yes

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→ heuristic

* Function estimates how close a state is to a goal.

* Designed for particular search problem.

* Ex: Manhattan distance

Greedy search

* strategy expand a node that you think is closest to a goal state.

↳ heuristic \Rightarrow estimate of distance to nearest goal for each state.

* Common Case

↳ best-first takes you to wrong goal

A* search

↳ only stop when we dequeue a goal.

Admissible Heuristics

↳ heuristic h is admissible (optimistic) if

$$0 \leq h(n) \leq h^*(n)$$

Where $\Rightarrow h^*(n)$ → is true cost to nearest goal.

UCS vs A* contours

UCS → expands ~~equally~~ in all "directions".

A* → expands mainly toward the goal but does hedge its bets to ensure optimality

A* Applications

video games, language analysis, speech ~~recognition~~,
recognition, machine translation, Pathing.

→ search problem consists of

1) state space

2) successor function
(with actions, costs)

3) start state and goal test.

solution → is sequence of actions (a plan)
which transform start state to goal state.